Math 128
Numerical Linear Algebra

Tufts University
Department of Mathematics

Sections: 01 (Block J+TR) Xiaozhe Hu
Office Hours: TR 9:30am-11:30am, or by appointment
Required Materials: Numerical Linear Algebra and Applications, Second Edition, by Biswa Nath Datta, published by SIAM Philadelphia.
In addition, there will be programming assignments that require the implementation of some computer language. The programming for this course can be done in any language that you choose. MATLAB is recommended and is probably the easiest to pick up if you are not familiar with any other. All Tufts students have access to MATLAB in the ITS Computing Center at Eaton Hall. Tufts University also provides Student License for MATLAB, you can follow the instruction on https://it.tufts.edu/sw-matlabstudent and install MATLAB on your own computers. An alternative to MATLAB is Octave. An possibility is Python with numpy/scipy/matplotlib. If you would like to use another option, please discuss this with me.
Recommended Reading Materials: Matrix Computations, Fourth Edition, by Gene H. Golub and Charles F. Van Loan, JHU Press and Numerical Linear Algebra, by Lloyd N. Trefethen and David Bau, III, SIAM Philadelphia.
Exams and Grading: The full department policy on exams and grading can be found on the department website http://math.tufts.edu/courses/examPolicy.htm, as well as the university's http://uss.tufts.edu/studentAffairs/documents/HandbookAcademicIntegrity.pdf. Students found violating these policies will receive an F in the course and be reported to the Dean of Students.
Student Accessibility Services: If you are requesting an accommodation due to a documented disability, you must register with the Student Accessibility Services Office at the beginning of the semester. To do so, call the Student Accessibility Services office at 617-6274539 to arrange an appointment with Linda Sullivan, Program Director of Student Accessibility Services.

Homework: There will be about 10 homework assignments during the semester. Some portions will involve programming. All codes should be printed and turned in with the resulting outputs. In addition, you should write up the answers based on the programming portion of the assignment in a report style, using figures and tables to justify your answers.
You are encouraged to collaborate with other students and to check your solutions. However, you must submit your own solutions in your own writing for the assignments.
Grades: Let M be your score on the midterm exam, F be your score on the final exam, and H be your total homework score. These are scores out of 100 . Your total course score will be the larger of the following two numbers:

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.3 H+.3 M+.4 F \quad \text { or } \quad .35 H+.1 M+.55 F \text {. }
$$

This score will be translated into a grade following a conversion table that you can find on the mathematics department web page, at http://math.tufts.edu/courses/gradingSchemes.htm.
Learning Objectives: This course satisfies Learning Objectives 1.b, 1.e, and 6.a as listed at http://ase.tufts.edu/faculty/committees/objectives/math.htm.

|  | Tentative Schedule |  |  |
| :---: | :---: | :---: | :---: |
| Lec. | Date | Book Sections | Topics |
| 1 | 01/15 | Sec 2.1-2.5 | Introduction and Review of Linear Algebra |
| 2 | 01/20 | Sec 3.1-3.8 | Floating Point Systems |
| 3 | 01/22 | Sec. 4.1-4.5 | Conditioning, Stability, and Accuracy |
| Homework 1 |  |  |  |
| 4 | 01/27 | Sec. 5.2-5.4 | LU Factorization |
| 5 | 01/29 | Sec. 7.1,7.5 | QR Factorization and Gram-Schmidt Process |
| 6 | 02/03 | Sec. 7.2,7.4 | Householder Transform and Givens Transform |
| Homework 2 |  |  |  |
| 7 | 02/05 | Sec. 9.1-9.5 | Eigenvalue Decomposition |
| 8 | 02/10 | Sec. 7.8-7.9 | Singular Value Decomposition (SVD) |
| Homework 3 |  |  |  |
| 9 | 02/12 | Sec. 6.4-6.7 | Solving Linear Systems, Direct Methods |
| 10 | 02/17 | Sec. 4.6, 6.8-6.9 | Perturbation Analysis and Condition Number |
| Homework 4 |  |  |  |
| 11 | 02/19 | Sec. 12.1-12.2 | Linear Iterative Methods |
| 12 | 02/24 | Sec. 12.3 | Krylov Methods |
| 13 | 02/26 | Sec. 12.4-12.5 | Preconditioning, Comparison |
| Homework 5 |  |  |  |
| Midterm (take-home) |  |  |  |
| 14 | 03/03 | Sec. 8.3, 8.5-8.6 | Least-Square Problems |
| 15 | 03/05 | Sec. 8.7.1-8.7.2 | Normal Equation, QR for Full-Rank Problems |
| 16 | 03/10 | Sec. 8.7.3-8.7.4 | QR for Rank-Deficient Problems, Using SVD |
| Homework 6 |  |  |  |
| 17 | 03/12 | Sec. 8.8 | Underdetermined Systems |
| 18 | 03/24 | Sec. 8.9 | Iterative Methods for Least-Square Problems |
| Homework 7 |  |  |  |
| 19 | 03/26 | Sec. 9.4, 9.6-9.7 | Eigenvalue Problems and Iterative Methods |
| 20 | 03/31 | Sec. 9.8-9.9 | The Real Schur Form and QR Iterations |
| Homework 8 |  |  |  |
| 21 | 04/02 | Sec. 10.2 | Symmetric Eigenvalue Problems |
| 22 | 04/07 | Sec. 12.6.1-12.6.2 | The Rayleigh-Ritz Procedure, Arnoldi Methods |
| 23 | 04/09 | Sec. 12.6.3 | Lanczos Methods |
| Homework 9 |  |  |  |
| 24 | 04/14 | Sec. 10.3.1-10.3.4 | SVD and Sensitivity |
| 25 | 04/16 | Sec. 10.3.5-10.3.7 | Computing SVD |
| Homework 10 |  |  |  |
| 26 | 04/21 | Sec. 10.4, 12.7-12.8 | Generalized Eigenvalue and SVD Problems |
| 27 | 04/23 |  | Review |
| Final Exam |  |  |  |

